

NAG C Library Function Document

nag_dpptri (f07gjc)

1 Purpose

nag_dpptri (f07gjc) computes the inverse of a real symmetric positive-definite matrix A , where A has been factorized by nag_dpptrf (f07gdc), using packed storage.

2 Specification

```
void nag_dpptri (Nag_OrderType order, Nag_UploType uplo, Integer n, double ap[],
                NagError *fail)
```

3 Description

To compute the inverse of a real symmetric positive-definite matrix A , this function must be preceded by a call to nag_dpptrf (f07gdc), which computes the Cholesky factorization of A using packed storage.

If **uplo** = **Nag_Upper**, $A = U^T U$ and A^{-1} is computed by first inverting U and then forming $(U^{-1})(U^{-1})^T$.

If **uplo** = **Nag_Lower**, $A = L L^T$ and A^{-1} is computed by first inverting L and then forming $(L^{-1})^T (L^{-1})$.

4 References

Du Croz J J and Higham N J (1992) Stability of methods for matrix inversion *IMA J. Numer. Anal.* **12** 1–19

5 Parameters

- 1: **order** – Nag_OrderType *Input*
On entry: the **order** parameter specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = **Nag_RowMajor**. See Section 2.2.1.4 of the Essential Introduction for a more detailed explanation of the use of this parameter.
Constraint: **order** = **Nag_RowMajor** or **Nag_ColMajor**.
- 2: **uplo** – Nag_UploType *Input*
On entry: indicates whether A has been factorized as $U^T U$ or LL^T as follows:
 if **uplo** = **Nag_Upper**, $A = U^T U$, where U is upper triangular;
 if **uplo** = **Nag_Lower**, $A = LL^T$, where L is lower triangular.
Constraint: **uplo** = **Nag_Upper** or **Nag_Lower**.
- 3: **n** – Integer *Input*
On entry: n , the order of the matrix A .
Constraint: $n \geq 0$.
- 4: **ap**[*dim*] – double *Input/Output*
Note: the dimension, *dim*, of the array **ap** must be at least $\max(1, n \times (n + 1)/2)$.

On entry: the upper triangular matrix U stored in packed form if **uplo** = **Nag_Upper** or the lower triangular matrix L stored in packed form if **uplo** = **Nag_Lower**, as returned by nag_dpptf (f07gdc).

On exit: U is overwritten by the upper triangle of A^{-1} if **uplo** = **Nag_Upper**; L is overwritten by the lower triangle of A^{-1} if **uplo** = **Nag_Lower**, using the same storage scheme as on entry.

5: **fail** – NagError *

Output

The NAG error parameter (see the Essential Introduction).

6 Error Indicators and Warnings

NE_INT

On entry, **n** = $\langle value \rangle$.

Constraint: **n** ≥ 0 .

NE_SINGULAR

Element $\langle value \rangle$ of the diagonal of the Cholesky factor is zero. The Cholesky factor is singular, and the inverse of A cannot be computed.

NE_ALLOC_FAIL

Memory allocation failed.

NE_BAD_PARAM

On entry, parameter $\langle value \rangle$ had an illegal value.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please consult NAG for assistance.

7 Accuracy

The computed inverse X satisfies

$$\|XA - I\|_2 \leq c(n)\epsilon\kappa_2(A) \quad \text{and} \quad \|AX - I\|_2 \leq c(n)\epsilon\kappa_2(A),$$

where $c(n)$ is a modest function of n , ϵ is the *machine precision* and $\kappa_2(A)$ is the condition number of A defined by

$$\kappa_2(A) = \|A\|_2 \|A^{-1}\|_2.$$

8 Further Comments

The total number of floating-point operations is approximately $\frac{2}{3}n^3$.

The complex analogue of this function is nag_zpptri (f07gwc).

9 Example

To compute the inverse of the matrix A , where

$$A = \begin{pmatrix} 4.16 & -3.12 & 0.56 & -0.10 \\ -3.12 & 5.03 & -0.83 & 1.18 \\ 0.56 & -0.83 & 0.76 & 0.34 \\ -0.10 & 1.18 & 0.34 & 1.18 \end{pmatrix}.$$

Here A is symmetric positive-definite, stored in packed form, and must first be factorized by nag_dpptrf (f07gdc).

9.1 Program Text

```

/* nag_dpptri (f07gjc) Example Program.
 *
 * Copyright 2001 Numerical Algorithms Group.
 *
 * Mark 7, 2001.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf07.h>
#include <nagx04.h>

int main(void)
{
    /* Scalars */
    Integer ap_len, i, j, n;
    Integer exit_status=0;
    NagError fail;
    Nag_UploType uplo_enum;
    Nag_OrderType order;

    /* Arrays */
    char uplo[2];
    double *ap=0;

#ifdef NAG_COLUMN_MAJOR
#define A_UPPER(I,J) ap[J*(J-1)/2 + I - 1]
#define A_LOWER(I,J) ap[(2*n-J)*(J-1)/2 + I - 1]
    order = Nag_ColMajor;
#else
#define A_LOWER(I,J) ap[I*(I-1)/2 + J - 1]
#define A_UPPER(I,J) ap[(2*n-I)*(I-1)/2 + J - 1]
    order = Nag_RowMajor;
#endif

    INIT_FAIL(fail);
    Vprintf("f07gjc Example Program Results\n\n");

    /* Skip heading in data file */
    Vscanf("%*[^\\n] ");
    Vscanf("%ld%*[^\\n] ", &n);
    ap_len = n * (n + 1)/2;

    /* Allocate memory */
    if ( !(ap = NAG_ALLOC(ap_len, double)) )
    {
        Vprintf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }

    /* Read A from data file */
    Vscanf(" ' %ls '%*[^\\n] ", uplo);
    if (*(unsigned char *)uplo == 'L')
        uplo_enum = Nag_Lower;
    else if (*(unsigned char *)uplo == 'U')
        uplo_enum = Nag_Upper;
    else
    {
        Vprintf("Unrecognised character for Nag_UploType type\n");
        exit_status = -1;
        goto END;
    }
    if (uplo_enum == Nag_Upper)

```

```

    {
        for (i = 1; i <= n; ++i)
        {
            for (j = i; j <= n; ++j)
                Vscanf("%lf", &A_UPPER(i,j));
        }
        Vscanf("%*[^\\n] ");
    }
else
    {
        for (i = 1; i <= n; ++i)
        {
            for (j = 1; j <= i; ++j)
                Vscanf("%lf", &A_LOWER(i,j));
        }
        Vscanf("%*[^\\n] ");
    }

/* Factorize A */
f07gdc(order, uplo_enum, n, ap, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from f07gdc.\\n%s\\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Compute inverse of A */
f07gjc(order, uplo_enum, n, ap, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from f07gjc.\\n%s\\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Print inverse */
x04ccc(order, uplo_enum, Nag_NonUnitDiag, n, ap,
        "Inverse", 0, NAGERR_DEFAULT);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from x04ccc.\\n%s\\n", fail.message);
    exit_status = 1;
    goto END;
}
END:
if (ap) NAG_FREE(ap);
return exit_status;
}

```

9.2 Program Data

f07gjc Example Program Data

```

4                               :Value of N
'L'                             :Value of UPLO
4.16
-3.12   5.03
0.56   -0.83   0.76
-0.10   1.18   0.34   1.18   :End of matrix A

```

9.3 Program Results

f07gjc Example Program Results

Inverse	1	2	3	4
1	0.6995			
2	0.7769	1.4239		
3	0.7508	1.8255	4.0688	
4	-0.9340	-1.8841	-2.9342	3.4978